Critical fields of the superconducting fullerene RbCs$_2$C$_{60}$

V. Buntar
Department of Physics, Parma University, I-43100 Parma, Italy
and Atomic Institute of the Austrian Universities, Schüttelstrasse 115, A-1020 Vienna, Austria

M. Riccò and L. Cristofolini
Department of Physics, Parma University, I-43100 Parma, Italy

H. W. Weber
Atomic Institute of the Austrian Universities, Schüttelstrasse 115, A-1020 Vienna, Austria

F. Bolzoni
Istituto MASPEC-CNR, I-43100 Parma, Italy
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The temperature dependence of the upper critical magnetic field $H_{c2}$ of the superconducting RbCs$_2$C$_{60}$ fullerene has been obtained. The value of $H_{c2}(0)$ at zero temperature is estimated to be 17 T and the coherence length $\xi(0) = 4.4$ nm. The lower critical field $H_{c1}$ has been studied using three different methods. The $H_{c1}(T)$ dependence obtained from the procedures based on the deviation from perfect diamagnetism and on Bean's critical-state model has a positive curvature with decreasing temperature. It is shown from a high-field analysis that this saturationless dependence does not reflect the intrinsic $H_{c1}$ of the superconductor. The value of $H_{c1}(0)$ is estimated to be 5.5–8.1 mT and the penetration depth $\lambda(0) = 300–370$ nm.

I. INTRODUCTION

Fullerene superconductors exhibit strong type-II superconductivity with a very large region of Shubnikov's mixed state, and their macroscopic magnetic properties are very similar to those of the high-$T_c$ oxides.$^{1–3}$ They are characterized by a large ($\sim 100$ nm) penetration depth and by a relatively small ($\sim 1$ nm) coherence length. There are three most important values of the magnetic field which can characterize the mixed state properties of a type-II superconductor: the lower critical field $H_{c1}$, at which the magnetic flux starts to penetrate a sample, the upper critical magnetic field $H_{c2}$, where the transition from the superconducting to the normal state occurs, and the thermodynamic critical field $H_c$. All of them can be evaluated from magnetization measurements. The knowledge of these critical fields leads then to the main characteristic superconducting length scales: the coherence length $\xi$ and the magnetic field penetration depth $\lambda$.

The thermodynamic critical field can be obtained from measurements of the reversible magnetization curve. However, in most cases the reversible magnetization is masked by flux pinning effects and, therefore, is not accessible. While there exist a few measurements of the reversible magnetization in the cuprate superconductors, the thermodynamic critical field of fullerenes has not yet been measured.

Regarding the upper and lower critical fields, there is a wide spectrum of different experimental techniques that can be used to evaluate $H_{c1}$. However, despite more than seven years of intensive investigations of $H_{c1}$, first for high-$T_c$ superconductors and then for the fullerenes, the values of the lower critical field and their temperature dependence are still controversial. This is especially true for fullerenes, since experimental data available on this new type of superconductors are scarce and the main superconducting characteristics of almost all of the fullerene superconductors are unknown.

In this paper we report on a determination of the temperature dependence of the upper and lower critical fields for superconducting RbCs$_2$C$_{60}$. The upper critical field was determined from the intersection between a linear extrapolation of the magnetization in the superconducting state and the normal-state base line. The lower critical field was determined from magnetization measurements using different procedures based on the first deviation from perfect diamagnetism, Bean's critical-state model, and on a high-field analysis of the reversible magnetization.

II. EXPERIMENT

Two samples were prepared and examined in our experiments. Sample 1 was prepared by thermal decomposition of azides.$^4$ Stoichiometric amounts of RbN$_{31}$, CsN$_{31}$, and pure C$_{60}$ were mixed and finely powdered in a mortar. The pressed powder was slowly heated above the decomposition temperature of the azides ($510–520^\circ$C) under dynamic vacuum. The decomposition was monitored by measuring the pressure ($N_2$ gas is developed in this process) and the heating was stopped as soon as it was restored to its initial value. $^{13}$C NMR at room temperature showed the presence of a peak centered at 177.5 ppm (with reference to tetramethyldisilane) with a width of
7 ppm half width at half maximum. No unreacted C$_{60}$ (peak at 143 ppm) was observed. The second sample of the same composition prepared by a similar procedure was also briefly characterized. Both samples have the same transition temperature $T_c = 33$ K, similar (about 40%) values of the shielding fraction at $T = 5$ K, and similar temperature dependence of the upper critical field.

The magnetic measurements of the first sample were performed with a high-sensitivity commercial superconducting quantum interference device (SQUID) magnetometer (Quantum Design) in fields up to 5.5 T and in the temperature range from 50 to 300 K. The second sample was measured with two SQUID magnetometers: a low-field magnetometer (Quantum Design) with a field range up to 1 T and a high-field magnetometer with a field range up to 8 T. The RbCs$_3$C$_{60}$ powder of both samples was sealed in a glass capsule under 1 bar of helium exchange gas. The powder can be approximated by a set of independent spheres. In this case the demagnetizing factor $n$ is equal to $1/3$ and the magnetic field inside the sample is related to the external magnetic field $H_{\text{ext}}$ by $H_{\text{in}} = H_{\text{ext}}/(1 - n)$.

### III. UPPER CRITICAL FIELD

The upper critical magnetic field was determined from the temperature dependence of the field-cooled (FC) magnetization. The experiment proceeded as follows. An external magnetic field (0.5 T $\leq H_{\text{ext}} \leq 5$ T) was applied at temperatures above $T_c$. The sample was then cooled down in $H_{\text{ext}}$ and the magnetic moment of the sample monitored at fixed $H_{\text{ext}}$ with increasing temperature from the superconducting to the normal state. The magnetization was reversible in the experimental temperature range 5 K $< T < T_c$. The transition temperature was estimated from the intersection between a linear extrapolation of the magnetization in the superconducting state and the normal-state base line. The upper critical field $H_{c2}$, for the temperature $T = T_c$, is equal to the applied external magnetic field, $H_{c2} = H_{\text{ext}}$. An example of such a measurement and the evaluation procedure of $H_{c2}$ from the experimental data for $H_{\text{ext}} = 1$ T are shown in Fig. 1. It is clear that the strong diamagnetic signal, which appears at $T = 30$ K, is due to the superconducting transition. A small paramagnetic signal in the normal state, which increases slightly with decreasing temperature down to $T = T_c$, indicates the existence of a nonsuperconducting paramagnetism in our sample. This is also confirmed by measurements of the hysteresis loops (see Fig. 6). This paramagnetism can be due to some nonstoichiometric impurities; its evaluation will be discussed in more detail in Sec. IV B.

The temperature dependence of the upper critical magnetic field near $T_c$ is shown in Fig. 2. The uncertainty in determining the transition temperature was not more than 1 K at any field. From the slope of $H_{c2}/8T = -0.8 \pm 0.1$ T/K and using the Werthamer-Helfand-Hohenberg (WHH) formula

$$H_{c2}(0) = 0.69(\delta H_{c2}/\delta T)T_c,$$

one can find for the upper critical magnetic field at zero temperature $H_{c2} = 17^{+3.2}_{-1.4}$ T. The value of the coherence length at zero temperature $\xi(0)$ can be obtained from $\xi(0) = (\Phi_0/2n\mu_0 H_{c2}(0))^{1/2}$ (where $\Phi_0 = h/2e$ is the flux quantum). This leads to $\xi(0) = 4.4^{+0.5}_{-0.3}$ nm. (The linear Ginzburg-Landau extrapolation gives $H_{c2}^{GL} = 25^{+7.3}_{-2.4}$ T and $\xi(0)^{GL} = 3.6^{+0.2}_{-0.1}$ nm.)

It is interesting to note that the upper critical magnetic field for the RbCs$_3$C$_{60}$ superconductor obtained in this work is much smaller than that for K$_3$C$_{60}$ (Ref. 1) or Rb$_3$C$_{60}$ (Refs. 2 and 3), while the coherence length is almost twice that obtained for those fullerenes. However, the value $\delta H_{c2}/8T = -1.7/K$, obtained for the Na$_2$N$_2$C$_{60}$ fullerene superconductor, is very close to that obtained in the present work. An enhancement of the upper critical field for powdered fullerene superconductors was discussed by Boebinger et al. 7 and several explanations were suggested. It was shown that the upper field critical fields might result in part from an orientational disorder between adjacent C$_{60}$ molecules, which limits the mean free path ($l_{\text{mfp}}$). In the dirty limit, where the Ginzburg-Landau coherence length $\xi_{GL}$ varies as $\xi_{GL} \sim (\xi_{GL} l_{\text{mfp}})^{1/2}$, where $\xi_{0}$ is the BCS coherence length, the limitation of the mean free path leads to a decrease of $\xi_{GL}$ and, therefore, to an increase of the upper critical field.

![FIG. 1. Magnetization vs temperature in an applied field $H_{\text{ext}} = 1$ T.](image)

![FIG. 2. Upper critical field $H_{c2}$ vs temperature. The solid line corresponds to a slope $\delta H/8T = -0.8T/K$.](image)
IV. LOWER CRITICAL FIELD

A. Deviation from the linear $M(H)$ behavior

The lower critical magnetic field $H_{c1}$ and hence the penetration depth $\lambda$ [provided the coherence length $\xi(0)$ is known from the measurements described above] can be determined from an experimental magnetization curve. In this work, the lower critical magnetic field was obtained from several methods. First, it was determined as the field at which a significant deviation of the $M(H)$ curve from linearity in the Meissner state was observed. As an example, Fig. 3 shows the magnetic field dependence of the magnetization at $T=10$ K, obtained by cooling the specimen from the normal state down to the indicated temperature under zero external magnetic field and by measuring the magnetization in increasing fields. We determine $H_{c1}$ as the field where the deviation from linearity sets in.

B. Bean critical-state model

In order to make this procedure more quantitative, it is tempting to apply Bean’s critical-state model\(^9\) for the entry of vortices into hysteretic superconductors. According to this theory, the magnetization is related to the critical current density $J_c$ (which is assumed to be field independent for simplicity), at fields above $H_{c1}$: $(M + H) \sim \langle H^2 - H_{c1}^2 \rangle / J_c D$, where $D$ is a characteristic length for the superconducting sample studied. (In our case, for a powder sample with a grain-size distribution from 0.2 to 3 $\mu$m, we expect $D$ to be of the order of the average grain size, $\sim 1 \mu$m.) This relation holds in the range $H_{c1}^2 < H < H^*$, where $H^* \sim J_c D$ is the field at which the flux penetrates the sample completely. Thus a plot of $\delta M$ vs $H^2$ [$H=H_{c1}/(1-n)$], where $\delta M = M + H_a$ is the deviation of the observed magnetization from perfect diamagnetic behavior, and in particular the threshold field of this plot, should give the lower critical field. Figure 4 shows a typical example of such a plot for our sample.

![Fig. 3](image1.png)

**Fig. 3.** Magnetization vs magnetic field at $T=10$ K.

![Fig. 4](image2.png)

**Fig. 4.** Deviation of the magnetization $\delta M = M + H_a$ vs $H_a^2$ at $T=10$ K.

C. Results and discussion

The temperature dependence of $H_{c1}$ obtained from these two methods is shown in Fig. 5 by the open symbols. In both cases, an anomalous saturationless temperature dependence with positive curvature at low temperatures is obtained. At 5 K the values of $H_{c1}$ are close to 20 mT and $H_{c1}$ decreases rapidly with increasing temperature to values of about 6 mT at about 12 K. For $T > 12$ K, $H_{c1}$ decreases almost linearly and the slope of $H_{c1}(T)$ is much smaller than at low temperatures. An extrapolation of this “high”-temperature linear dependence to zero temperature gives a value of $H_{c1}(0)$ of around 7.5 mT. At the same time, the “high”-temperature data can be described well by a parabolic dependence $H_{c1}(T)/H_{c1}(0) = 1 - (T/T_c)^2$ (solid line in Fig. 5), which leads to $H_{c1}(0) = 5.5$ mT. The penetration depth $\lambda(0)$ calculated from $H_{c1} = 5.5$ mT with the relation\(^10\)

![Fig. 5](image3.png)

**Fig. 5.** Lower critical field $H_{c1}$ vs temperature. The open circles correspond to data obtained from the deviation from perfect diamagnetism; triangles, data from the analysis based on Bean’s critical-state model; closed circles, data from the high-field analysis. The dashed lines show linear extrapolation of the data obtained from the first two methods at low ($< 12$ K) and high ($12 < T < T_c$) temperatures. The solid line corresponds to $H_{c1}(T) = H_{c1}(0)[1 - (T/T_c)^2]$, with $\mu_0 H_{c1}(0) = 5.5$ mT.
\( \mu_0 H_{c1}(0) = (\phi_0 / 4\pi \lambda^2) \ln(\lambda / \xi) \) is \( \lambda(0) = 370 \) nm.

A similarly anomalous dependence of the lower critical magnetic field was observed for high-\( T_c \) superconductors. For instance, it has been reported for single crystals of YBa\(_2\)Cu\(_4\)O\(_{7-\delta}\) (Refs. 11–13), Bi-2212 (Ref. 14), Tl-2212 (Ref. 15), \( Pb_2Sr_2R_1-xCa_xCu_3O_{7+y} \) (Ref. 16), ceramics of (Bi,Pb)-2223 (Ref. 17), and \( S/N \) layered superconductors.\(^{18}\)

There are at least five possible ways to explain this anomalous behavior. First, the effect could be due to the existence of a second superconducting phase with lower \( T_c \) and higher \( H_{c1} \). In our specimen there could be two coexisting superconducting compounds in the case of sample inhomogeneities. They could be the \( Rb_3\)Cs\(_{60}\) and the \( Rb_2\)Cs\(_{60}\) compounds with critical temperatures of about 28 and 31 K, respectively. However, the slope of \( M(T) \) in the Meissner state does not show any significant changes at these temperatures indicating a constant shielded volume. Moreover, the upper critical fields for these compounds are much larger (see, for instance, Ref. 19) and their influence would be seen in the \( H_{c2}(T) \) dependence. The slope \( \delta H_{c2}/\delta T \) obtained in this work remains very small, in comparison with \( \delta H_{c2}/\delta T \) for the \( Rb_3\)Cs\(_{60}\) compounds\(^{19}\) down to 23 K (see Fig. 2) and does not exhibit any significant changes. Therefore, we can confidently conclude that we do not detect any other superconducting phases in our sample except for \( Rb_3\)Cs\(_{60}\).

The second possibility which could be considered is the existence of intergranular regions and different types of defects inside the grains. The similar temperature behavior obtained for single crystals (see references above) confirms, however, that this is not a property of granular and ceramic superconductors, making this explanation less plausible.

In a number of papers, theoretical and experimental results were presented explaining such a \( H_{c1}(T) \) behavior as an intrinsic property of layered superconductors.\(^{18,20,21}\)

For our sample, where the superconducting fraction is about 40%, such a superconducting-non-superconducting structure could be an explanation of the anomalous temperature dependence of the lower critical field. However, it was shown\(^{18}\) that it is very important for this situation to have the external magnetic field perpendicular to the layers. This cannot be expected for our sample, which certainly has a random distribution of superconducting and nonsuperconducting regions.

One further explanation was suggested in Ref. 13, where the authors explained the positive curvature of \( H_{c1}(T) \) by the existence of a Bean-Livingston surface barrier.\(^{22}\) The appearance of these barriers at low temperatures is more likely than at high ones, because the higher the temperature, the more easily the surface barrier can be overcome by thermal fluctuations.

Finally, it should be kept in mind that the deviation of the \( M(H) \) curve from linearity is significantly smaller at low temperatures and that the determination of such small deviations is already a matter or resolution of the experimental method. This can lead to much higher values of \( H_{c1} \) obtained at low temperatures from magnetization measurements with highly sensitive SQUID magnetometers.\(^{23}\)

The last two explanations of the experimental data are most likely. But whatever the nature of the positive curvature of \( H_{c1}(T) \) is, the anomalous increase of \( H_{c1} \) at low temperature does not reflect the behavior of the intrinsic \( H_{c1} \). The "real" \( H_{c1} \) at zero temperature should be much lower than the 20 mT obtained above according to the high-temperature data.

### D. High-field analysis

In order to find the real lower critical magnetic field one can use a high- and intermediate-field analysis, where \( H_{c1} \) can be estimated from the values of the penetration depth \( \lambda \), the coherence length \( \xi \), and the Ginzburg-Landau parameter \( \kappa \). This avoids the influence of the Bean-Livingston barrier and is more accurate than that based on low-field measurements, especially in the case of inhomogeneous samples with a low superconducting fraction.\(^{24}\)

The key point is the determination of \( \kappa \) and \( H_{c1} \) on the basis of data obtained at high \( (H \leq H_{c2}) \) and intermediate \( (H_{c1} << H << H_{c2}) \) external magnetic fields. According to the Ginzburg-Landau theory, the reversible magnetization for \( H \leq H_{c2} \) is given by\(^{25}\)

\[
-M = \frac{H_{c2}(T) - H}{\lambda(2\lambda^2 - 1)\beta_a},
\]

where \( \beta_a = 1.16 \). Since \( \kappa = \lambda / \xi \), we can estimate \( \lambda \) and \( H_{c1} \) from the reversible \( M(H) \) dependence, provided the coherence length is known from independent experiments on \( H_{c2} \). For \( H_{c1} << H << H_{c2} \),\(^{25}\)

\[
-M = \frac{\kappa \phi_0}{8\pi\lambda^2(T)} \ln \frac{\beta H_{c2}(T)}{H}.
\]

In our experiments we have measured the magnetization in fields up to 5.5 T at different temperatures up to 30 K, close enough to \( T_c \). For our experimental magnetic field window, a reversible region of \( M(H) \) was found at temperature \( T > 20 \) K. Typical \( M(H) \) dependences at \( T > 20 \) K are shown in Fig. 6. The reversible region was found at fields higher than 4 T (for \( T = 24 \) K), 3.2 T (\( T = 25 \) K), 2.2 T (\( T = 27 \) K), 1 T (\( T = 29 \) K), and 0.5 T (\( T = 30 \) K). For all these temperatures, \( H_{c1} / H_{c2} > 0.4 \) (where \( H_{c1} \) is the reversibility field). This means that the reversible region in our experiments occurs in the high-field regime and Eq. (1) (Ref. 26) should be used.\(^{27}\)

Figure 6 demonstrates that nonsuperconducting paramagnetism is significant in our sample and its contribution, \( M_p \), to the total measured magnetization, \( M \), should be taken into account when evaluating the magnetization \( M_{sc} \) produced by the persistent currents. On the other hand, the sample magnetization is related to the magnetization of a perfect superconductor via the superconducting fraction \( x \):

\[
M_e = xM + \chi_H H.
\]

The shielding fraction \( x_{sh} \), which is not equal, in general, to the superconducting one\(^{24,28}\) was evaluated for
different temperatures from the slope of the $M(H)$ dependencies. Since in a perfect superconductor $M = -H$, the following definition for $x_{sb}$ was adopted: $x_{sb} = -dM/\delta H$. The shielding fraction $x_{sb}(T)$ thus evaluated is around 40%.

The magnetic field dependence of the superconducting magnetization,

$$ M_{sc} = \frac{M - \chi_p H}{\kappa} $$

[see Eq. (3)] is shown in Fig. 7 for different temperatures. As it should be, these dependences are linear in the high field ($H \leq H_{c2}$) region. The slope is $\delta M_{sc}/\delta H = \chi / [(2\kappa^2 - 1)\beta_p]$, from which $\kappa$ can be evaluated. This results in $\kappa = 65.6, 58, 67.7, 76.6,$ and 66.3 from the $M_{sc}(H)$ dependences at 24, 25, 27, 29, and 30 K, respectively. That leads to an average value $\kappa = 67 \pm 10$, $\lambda(0) = 300 \pm 50$ nm, and the lower critical field at zero temperature $\mu_0 H_{c1}(0) = 8.1 \pm 2$ mT. This value is close to that ($m_0 H_{c1} \approx 7.5$ mT) obtained from the linear approximation of the "high" temperature dependence in Fig. 5. It confirms our proposal that the positive curvature of $H_{c1}(T)$ does not reflect the intrinsic value of the lower critical field at low temperatures.

From the values of $\kappa$ and $\lambda(0)$ obtained from the linear dependences in Fig. 7, one can find the values of $\lambda(T)$ and then $H_{c1}(T)$ using the two-fluid relation,

$$ \lambda(T) = \lambda(0)[1 - (T/T_c(0))^4]^{-1/2}, $$

which gives good agreement with experimental results for other fullerene superconductors.24,29 The values of $H_{c1}$ obtained in this way for $T = 24, 25, 27, 29, $ and 30 K are plotted in Fig. 5 (full circles) and show good agreement with the data obtained from the low-field analysis at high temperatures.

V. SUMMARY

The temperature dependence of the upper critical magnetic field $H_{c2}$ and the value of the coherence length $\xi$ at room temperature were obtained for the superconducting RbCs$_2$C$_{60}$ fullerene. The upper critical field at room temperature is estimated to be $H_{c2} = 17$ T with a slope $\delta H/\delta T = -0.8$ K. The lower critical magnetic field was obtained by three different methods. It is shown that two of them [evaluation of $H_{c1}$ from the point of the first significant deviation from the linear $M(H)$ dependence and from the Bean critical-state model] give a saturationless temperature dependence with positive curvature at low temperatures and do not reflect the real intrinsic lower critical field of the superconductor. On the other hand, the high-field analysis for the determination of $H_{c1}$ gives significantly smaller values of the lower critical field at zero temperature $[\mu_0 H_{c1}(0) = 8.1$ mT] and, at the same
time, shows very good agreement with the other methods at $T > 0.5 T_c$. For these temperatures, experimental data obtained by all methods can be described by a parabolic dependence, $H_{c1}(T)/H_{c1}(0) = 1 - (T/T_c)^2$, which leads to $H_{c1}(0) = 5.5$ mT. The corresponding values of the penetration depth $\lambda(0)$ are $\lambda(0) = 300$ nm and $\lambda(0) = 370$ nm.

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In order to check this supposition, we also analyzed our data using the logarithmic equation [Eq. (2)]. The data obtained at 24 and 25 K also give good agreement with Eq. (2) and lead to similar values for the penetration depth at zero temperature ($\lambda \approx 300$ nm), while the data obtained at 29 and 30 K do not fit the logarithmic behavior.